

STUDY GUIDE:

PHYSICS SL



IB Academy Physics Study Guide

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INTRODUCTION

Welcome to the IB. Academy Study Guide for Physics.

We are proud to present our study guides and hope that you will find them helpful. They are the result of a collaborative undertaking between our tutors, students and teachers from schools across the globe. Our mission is to create the most simple yet comprehensive guides accessible to IB students and teachers worldwide. We are firm believers in the open education movement, which advocates for transparency and accessibility of academic material. As a result, we embarked on this journey to create these study guides that will be continuously reviewed and improved. Should you have any comments, feel free to contact us.

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1.1 Physical measurements

1.1.1 Fundamental and derived SI units

Fundamental units

There are six fundamental SI units from which all other units can be derived.

Time	seconds	s
Displacement	meters	m
Mass	kilograms	kg
Temperature	kelvin	K
Amount of substance	mole	mol
Current	ampere	A

Derived units

All other units can be expressed as a combination of these fundamental units, therefore derived from them.

mple.

Since speed =
$$\frac{\text{displacement}}{\text{time}}$$
, or $v = \frac{s}{t}$, the units for v are $\frac{\text{unit of displacement}}{\text{unit of time}} = \frac{[m]}{[s]} = m s^{-1}$

In a similar manner we can derive other units:

• Force = Mass × Acceleration = $[kg] \times [m s^{-2}]$, therefore the unit is $kg m s^{-2}$.

$$1 \text{ kg m s}^{-2} = 1 \text{ N}$$
, or newton.

• Pressure = $\frac{\text{Force}}{\text{Area}} = \frac{[\text{kg m s}^{-2}]}{[\text{m}^2]}$, therefore the unit is kg m⁻¹ s⁻².

$$1 \text{ kg m}^{-1} \text{ s}^{-2} = 1 \text{ Pa}$$
, or pascal.

• Energy = Force \times Distance, therefore the unit is kg m² s⁻².

$$1 \text{ kg m}^2 \text{ s}^{-2} = 1 \text{ J}$$
, or joule.



Write the compound units as a combination of SI units

Compound quantity		Calculation	Derived unit
Power	[watt]	$P = \frac{E}{t}$	
Charge	[coulomb]	$Q = A \times t$	
Resistance	[ohm)	$R = \frac{V}{I}$	
Magnetic field strength magnetic flux density	[tesla]	$B = \frac{F}{IL}$	

1.1.2 Orders of magnitude



Order of magnitude a method of comparing the sizes of values, with each order of magnitude being equivalent to a multiple of 10.

Metric multipliers prefixes that precede units to indicate its order of magnitude.

As an example, the order of magnitude of 1500 is 3, and in scientific notation it will be written as 1.5×10^3 . Meanwhile, 0.1 is 2 orders of magnitude smaller than 10, since it is 100 times smaller than 10.

One can also use prefixes to indicate the order of magnitude of a unit. So, 1000 m is 1 km, while 2×10^{-3} J is equal to 1 mJ. The SI prefixes used by IB can be seen in Table 1.1.

DB page 2

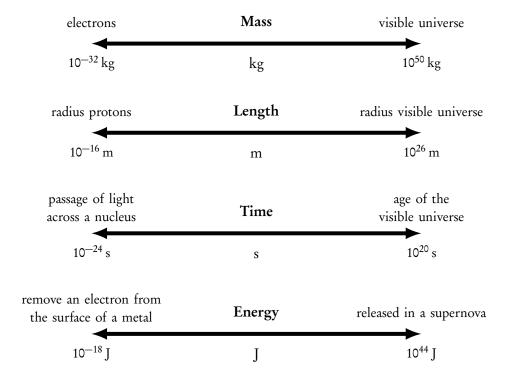
Table 1.1: Metric (SI) multipliers

Prefix	Symbol	Power	Prefix	Symbol	Power
yocto	y	10 ⁻²⁴	deca	da	10 ¹
zepto	z	10^{-21}	hecto	h	10^{2}
atto	a	10^{-18}	kilo	k	10^{3}
femto	f	10^{-15}	mega	M	10 ⁶
pico	р	10^{-12}	giga	G	10 ⁹
nano	n	10 ⁻⁹	tera	T	10 ¹²
micro	μ	10 ⁻⁶	peta	P	10^{15}
milli	m	10^{-3}	exa	E	10^{18}
centi	c	10^{-2}	zetta	Z	10^{21}
deci	d	10 ⁻¹	yotta	Y	10 ²⁴

1.1.3 Estimation of quantities

To show your understanding of both the SI units and the orders of magnitude, IB often tests your knowledge of these in a paper 1 exam, relating values dealing with atoms to astronomical objects and events.

It is important to have a general awareness what scales such objects deal with.





1.1.4 Significant figures

Significant figures are used to show the accuracy of a measurement.

Determination of the number of significant figures can be summarised with the following rules.

- 1. Non zero digits are significant, e.g. 4.643 has 4 significant figures: 4.643
- 2. Zero digits between non-zero digits are significant, e.g. 809 has 3 significant figures: 809
- 3. Zero digits after a decimal are significant if they lie to the right of a non-zero digit, e.g. 4.000 and 0.03200 both have 4 significant figures: 4.000 0.03200
- 4. All other zero digits are *not* significant, e.g. 0030 has 1 significant figure: $00\frac{1}{3}0$

To ensure you get your significant figures correct, make sure you look at your calculations with the two definitions shown below.

- 1. When multiplying or dividing, check which given value used in your calculations has the least number of significant figures.
 - This should be the number of significant figures in your answer, e.g. $1.34 \times 4.8 = 6.432$ should be expressed as 6.4 because 4.8 has only 2 significant figures.
- 2. When adding or subtracting, check which given value used in your calculations has the least number of decimal places.
 - This should be the number of decimal places your answer, e.g. 7.34 + 4.8 = 12.14 should be expressed as 12.1 because 4.8 has only 1 decimal place, even though this exceeds the number of significant figures in 4.8.
- 3. If one of the given values comes from a graph:
 - Use the amount of significant figures corresponding to the smallest grid on the graph,
 - e.g. for a graph grid units of 0.1, a reading such as 3.65 should be expressed to only 2 significant figures, as 3.6.

Determine the number of significant figures in the following values

1. 102

3. 2.0×10^{-2}

2. 0.00235

4. 314.159



1.2 Uncertainties and errors

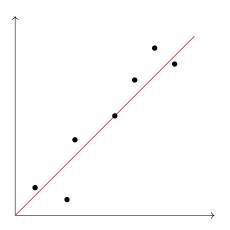
Errors have always been a part of experiments as you've likely encountered in practicals. It is important to deal with this in calculations, which can be done using a set of simple rules explained in the next few sections.

1.2.1 Random and systematic errors

These types of errors should not be confused with simple mistakes such as misreading an instrument, writing down the wrong number or making a calculation error, which are not considered sources of experimental error.

Random errors

Affects each measurement in a random manner.



Leads to a less precise experiment.

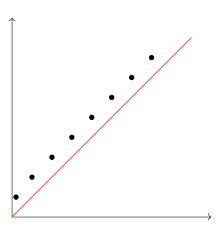
Caused by fluctionations in the instrument readings, observer interpretation and effects due to changes in the surroundings.

Reduced by repeated readings.

Data points are spread around the perfect data, the more measurements made the closer the data matches the perfect results.

Systematic errors

Affects each measurement in the same way.



Lead to a less accurate experiment.

Caused by wrongly calibrated apparatus and imperfect methods of observation.

Reduced by ensuring instruments are properly calibrated, by mathematically removing known offsets, or by changing the way a measurement is taken. Data is either proportional to the perfect results, or deviating by some constant value. By checking the y-intercept the size of the error can be determined.



1.2.2 Absolute, fractional, and percentage uncertainties

Turn off your intuitive perception on uncertainties and allow your mathematical side to come to life. When approached with a simple mathematical formula, calculating the uncertainty will become a routine procedure. Moreover, it will also help your understanding of the uncertainty of the compound or calculated values.



Absolute uncertainty the uncertainty in a measurement as an absolute value, e.g. ± 0.5

Fractional (relative) uncertainty the uncertainty in a measurement as a fraction of the measurement, given by $\frac{\text{absolute uncertainty}}{\text{measurement}}$.

Percentage uncertainty the fractional uncertainty in a measurement expressed as a percentage, given by fractional uncertainty \times 100%, e.g. \pm 0.5%

The following rules are given in the data booklet and are all the manipulations you will need to know for your exams.

Note that when expressing a measurement, use only an absolute or percentage uncertainty (to avoid a fractional uncertainty being confused for an absolute uncertainty). Fractional uncertainties are used in intermediate calculations.

DB St 1.2 (p4)

Addition and subtraction: y = a + b and y = a - b

The uncertainty after addition/subtraction is the *sum* of the *absolute uncertainties* of *a* and *b*.

$$\Delta y = \Delta a + \Delta b$$

Multiplication and division: $y = \frac{ab}{c}$

The uncertainty after multiplication/division is the *sum* of the *fractional* uncertainties of a, b and c.

$$\frac{\Delta y}{y} = \frac{\Delta a}{a} + \frac{\Delta b}{b} + \frac{\Delta c}{c}$$

where $\frac{\Delta y}{y} = \%$ fractional uncertainty.

Exponential: $y = a^n$



The uncertainty after an exponent n is the *multiplication* of the *fractional* uncertainty by the power n.

$$\frac{\Delta y}{y} = \left| n \frac{\Delta a}{a} \right|$$

If the absolute uncertainty is defined as 1 cm when measuring your height to be 2 m then the percentage uncertainty is 0.5%.

$$\frac{1 \text{ cm}}{200 \text{ cm}} \times 100\% = 0.5\%$$

If the absolute uncertainty is 8 cm when measuring Kim's height to be 160 cm then the fractional uncertainty is $\frac{8}{160} \times 100 = \frac{1}{20} \times 100$ which corresponds to a percentage uncertainty of 5%.

- 1. What would the fractional uncertainty of Bill's measurement be if he is measured at 200 cm with an absolute uncertainty of 8 cm?
- 2. If Kim were to stand on Bill's head what would you estimate their combined height to be?

Often, the question will ask you to find the absolute uncertainty in the solution, Δy . Typically you are given absolute uncertainties but sometimes the IB can be tricky and give you the percentage uncertainty, so pay close attention.

Uncertainties from Graphs

Samir accelerates constantly and his velocity v increases according to the graph below. The accelerometer used isn't perfect and this is represented by the error bars.

$$v \text{ (m s}^{-1})$$

7

6

5

4

3

1 2 3 4 5 6 7 8 time (s)

If Samir exerts an average force $F = (1000 \pm 100) \, \text{N}$ per stop, how much power does Samir generate at $t = 4 \, \text{s}$? Use $P = F \, v$.

Let $a = 2 \pm 0.5$ and $b = 5 \pm 1.2$.

- 1. Calculate the uncertainty in c = a + b.
- 2. Calculate the uncertainty in c = ab.



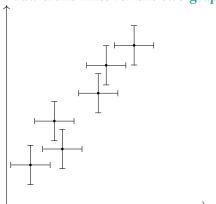
Drawing a trend line

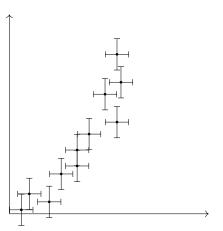
Questions regarding uncertainty may also be shown graphically using error bars. A typical question the IB may ask is to draw a line of best-fit. When drawing this line, you should *always* keep these very important rules in mind.

- 1. Identify whether the points follow a linear or non-linear progression.
- 2. Always! Start at the origin.
- 3. Draw your trend-line ensuring you go through all error bars.

Exercit







Finding the gradient of a line

The gradient of a straight-line graph represents how fast the dependent quantity changes in relation to the independent quantity, e.g. a gradient of 2 means that for every 1 unit on the x axis, the y value changes by 2.

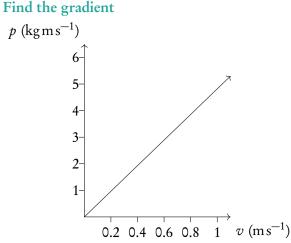
The gradient can be determined by picking two points on the line (as far apart as possible, to reduce error). For two points (x_1, y_1) and (x_2, y_2) , the gradient m is given by

$$m = \frac{y_2 - y_1}{x_2 - x_2}$$

The point where the line cuts the y axis is known as the intercept and is usually denoted c.



Thus we can write the equation of the line y = mx + c, which links the dependent variable to the independent variable.



What does the gradient represent in this example?

1.3 Vectors

Usually, the image you get when you hear the word vector is an arrow pointing in a certain direction. To picture the arrow you need to know its direction and its length. In physics, we assign a physical meaning to the length of a vector, for example the magnitude of a force. In this way, the vector can be used to represent a force of a particular magnitude operating in a particular direction. In the IB, you will be using vectors in nearly every topic and you will see that they actually make life much easier by allowing you to combine quantities that would be tedious to work with as components. Vectors also allow you to quickly draw a diagram of almost any physical situation and thus develop some intuition regarding what is going on.

1.3.1 Vectors and scalars



A vector is defined as a quantity which has both a magnitude and a direction.

A scalar is defined as a quantity which has only a magnitude *without* any associated direction.



For example, speed is a quantity that has a magnitude and units (m s⁻¹) but has no direction associated with it. Its vector counterpart is velocity, which does have a direction.

Name three vector quantities and three scalar quantities.

1.3.2 Combination and resolution of vectors

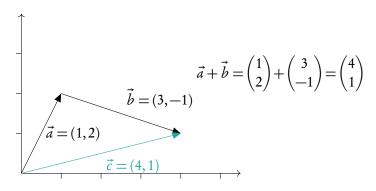
While vectors are similar to scalars in that you can add and subtract them, the exact procedure by which this is done is somewhat different since you need to take the vector's direction into account.

The techniques outlined in this section are all the necessary ones for vector calculations in IB physics.

Mathematical vector manipulation

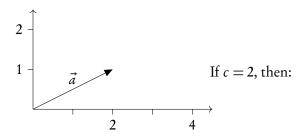
Addition and subtraction of vectors

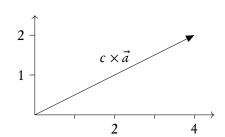
Imagine there are two displacement vectors, \vec{a} and \vec{b} . We can find their sum if we connect the tail of the one to the point of the other. It does not matter in which order we add the vectors. Note if you go along the opposite direction of a vector its positive values are negative and vice versa.



Multiplication and division of vectors by scalars

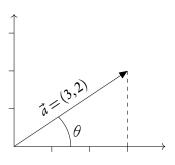
If I have a vector \vec{a} and multiply it with a scalar c, then the result is simply $c \cdot \vec{a}$, i.e.:





Trigonometric form

Especially in topics like mechanics, there will be cases where you'll need to split a vector into two parts, generally into a vertical and horizontal part. To do this you need the magnitude of your vector and the angle θ it makes with the x-axis. Your data booklet contains a diagram that shows how to find the component form of a vector



$$\hat{x} = 3 \qquad \hat{y} = 2$$

$$|\vec{a}| = \left(x^2 + y^2\right)^{\frac{1}{2}}$$

$$= (9 + 4)^{\frac{1}{2}} = \sqrt{13}$$

$$\theta = \arctan\left(\frac{y}{x}\right)$$

$$= \arctan\left(\frac{2}{3}\right) = 33.7^{\circ}$$



MECHANICS



2.1. Motion- Displacement, velocity, acceleration & the equations of motion - Graphs describing motion - Terminal velocity	
2.2. Forces - Newton's laws of motion - Solid friction	
2.3. Work, energy, and power - Kinetic, gravitational, and elastic potential energy & the principle of conservation of energy – Work done as energy transfer – Power as rate of energy transfer & efficiency	
2.4. Momentum and impulse - Newton's 2 nd law & force-time graphs	



2.1 Motion

We want to describe how bodies move through space by considering their displacement, velocity and acceleration over periods of time. Keep in mind that all of these are vector quantities and so we need to keep their direction in mind!

2.1.1 Displacement, velocity, acceleration & the equations of motion



Displacement a vector quantity stating the distance removed from a reference point.

Velocity a vector quantity stating the rate of change of the displacement.

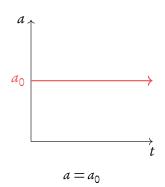
Acceleration a vector quantity stating the rate of change of the velocity.

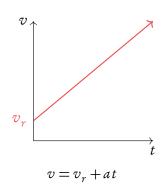
Within the IB, we will always approach problems under the assumption of uniform motion. If this is not the case, the IB will explicitly state this in the beginning of a problem!

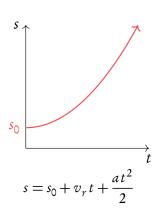
Uniform motion the motion of a body under constant (possibly zero) acceleration.

Typically, you will be asked to find instantaneous values for velocity, speed, and acceleration either from graphs or using the *equations of motion*.

DB The equations of motion are:









$$\vec{v}_{av} = \frac{\vec{u} + \vec{v}}{2}$$
 $\begin{pmatrix} \vec{u} = \text{initial velocity} \\ \vec{v} = \text{final velocity} \end{pmatrix}$

In the IB exams, occasions will arise where both the observer and the target are moving, which means that we are dealing with relative velocity. In this case, the velocity \vec{v} of the target is the sum of the observer's velocity $\vec{v}_{\rm o}$ and the targets velocity with respect to the observer \vec{v}_{r} .

$$\vec{v} = \vec{v}_0 + \vec{v}_r$$

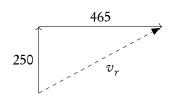


Relative velocity between two bodies is the velocity of one body in the rest frame of the other.

Imagine you're flying upwards at $v_f = 250 \,\mathrm{m\,s^{-1}}$ perpendicular to the Earth's rotation, with the Earth spinning at $v_{\rm E} = 465 \,\mathrm{m\,s^{-1}}$ to the right.

An astronaut at the ISS is measuring how fast you're going.

What's your relative speed, v_r ?
First we draw the two velocity vectors and place them end to end like below.



Since the two vectors form a right triangle, we can find the \boldsymbol{v}_r by Pythagoras' theorem.

$$v_r = \sqrt{(250)^2 + (465)^2}$$

= $\sqrt{62500 + 216225}$
 $\approx 528 \,\mathrm{m \, s}^{-1}$

What is the direction θ of the velocity with respect to the Earth's rotation? To find the angle θ , we use that $\tan(\theta) = \frac{v_f}{v_E}$. Therefore, the angle θ is: $\theta = \arctan\left(\frac{250}{465}\right) \approx 28^\circ$

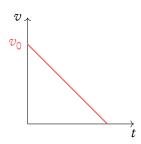


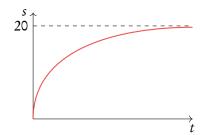
2.1.2 Graphs describing motion

For the following graphs, you will be given various scenarios. Draw the corresponding displacement and velocity curves on the axes given. The first one has been done for you as an example.

ample.

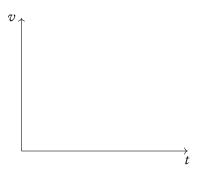
A car is coming to rest at constant deceleration from velocity v_0 , it takes the car 20 m to come to a halt from $S_0 = 0$.

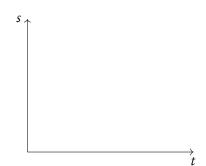




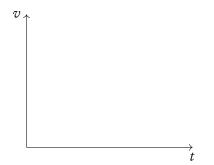
ercize

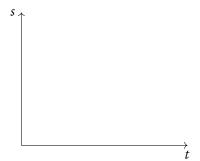
A bullet fired at a wall at constant velocity v_0 . The bullet travels 50 m before it hits the wall.





A ball rolls down a hill and then up another, coming to rest at the top of the hill. Assume acceleration from gravity.





2.1.3 Terminal velocity

To conclude motion, we will spend a little time talking about the consequences of fluid resistance. As mentioned in the beginning, in the IB all problems are approached under the assumption of negligible air resistance. However, sometimes you will be asked to explain in words or pictures what happens if we do take it into account.

Terminal velocity the constant speed that a freely falling object eventually reaches when the resistance of the medium through which it is falling prevents further acceleration.

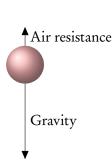
To get a better understanding, we will regard the situation of an object dropping from an arbitrary height towards earth. When the object is first dropped, it has zero velocity, as it is not moving there is also no resistance force. However, as the object starts dropping it starts moving faster.

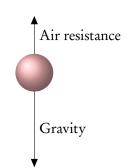
Air resistance is an exponential consequence of motion, as the object starts moving faster, it will experience a greater resistance force. At a certain point, the object will stop increasing in velocity and continue falling at *terminal velocity*. At this point, the air resistance is so great that it is equal to the force of gravity, but in the opposite direction! It follows that the net force on the object is zero and thus it will no longer increase in velocity.

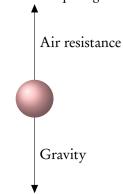
Ball starts accelerating due to gravity.

Ball continues accelerating, air resistance increases.

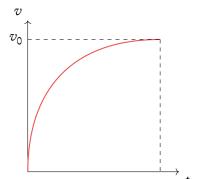
Ball reaches terminal velocity, when air resistance equals gravity.







If we plot the change in velocity over time, we get something that looks like this:



2.2 Forces

Force is the vector quantity most often used in IB physics. Typically, we regard the object in question as a point particle. This assumption basically allows one to take the object as a whole and not as a rigid body. We've already seen an example of an object being regarded as a point particle within the context of a force diagram when looking at terminal velocity in the previous section.

In mechanics, we will only be considering two forces, deformation and changes in velocity.



A force is a push or a pull that causes a change in magnitude *and/or* direction of velocity.

Point particle is an object represented as a point, ignoring that it is in fact a rigid body.

2.2.1 Newton's laws of motion

Although forces can be interpreted rather intuitively, we should follow a certain set of rules to describe such a fundamental concept.

Fortunately for us, these sets of rules have been well established by Isaac Newton in 1687.



Newton's 1^{st} Law If the force F on an object is zero then its velocity v is constant.

$$F_{\text{net}} = 0 \Rightarrow \frac{\Delta v}{\Delta t} = 0$$

Newton's 2^{nd} Law The force F of an object is equal to its mass m times its acceleration a.

$$F = ma$$

$$F = force [N]$$

$$m = mass [kg]$$

$$a = acceleration [m s-2]$$

Newton's 3rd Law Every action has an equal but opposite reaction.

$$\vec{F}_a = -\vec{F}_b$$



2.2.2 Solid friction

Friction arises whenever one body slides over another, or whenever there is a tendency for motion.

Dynamic friction

The force of dynamic friction is equal to:

$$F_d = M_d R$$
 $R = \text{normal reaction force}$ [N] $M_d = \text{coefficient of dynamic friction dimensionless}$

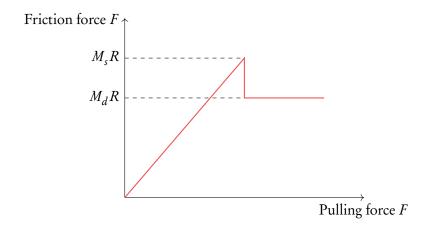
Note that the force of dynamic friction does not depend on the speed of sliding.

Static friction

The maximum force of static friction that can develop between two surfaces is given by:

$$F_s = M_s R$$
 $R = \text{normal reaction force}$ [N] $M_d = \text{coefficient of static friction dimensionless}$

Note that $M_s > M_d$.



2.3 Work, energy, and power

Out of all the various concepts in physics, energy is the most universal. It is present in many different forms and can also transform between its various forms.

In mechanics, we regard three forms of energy:

- 1. Kinetic energy
- 2. Gravitational potential energy
- 3. Elastic potential energy

As we move to other topics, we will encounter other forms of energy and how we transform between them.

2.3.1 Kinetic, gravitational, and elastic potential energy & the principle of conservation of energy

We will always be regarding transformations between kinetic and potential energy. Whether the potential energy is stored as gravitational or elastic is arbitrary.

In equation form, the three types of energy may be written as:

kinetic	$E_k = \frac{1}{2}mv^2$
gravitational	$E_g = mgh$
elastic	$E_e = \frac{1}{2}kx^2$



Principle of conservation of energy states that in any closed system, total energy will always be conserved or stay constant.

When regarding transformations in energy, we may assume that in a closed system, the total energy is conserved.



DB

Conservation of energy

Imagine the situation where Bryan and Lucy are standing on the same cliff and want to jump into the water at the same time. If Bryan jumps as high as he can while Lucy dives straight down, assuming they jump at the same initial speed, who will hit the water with a greater velocity?

If Bryan and Lucy both weigh 60 kg they jump at 5 m/s.

- 1. What is the maximum height Bryan will reach if the cliff is 10 m above the water?
- 2. With what velocity will each of them hit the water?

2.3.2 Work done as energy transfer



Work is the amount of force exerted in the direction of motion.

$$W = F s \cos \theta$$
 $W = \text{work}$ [J]
 $F = \text{force}$ [N]
 $S = \text{direction}$ [m]

 θ is the angle between the force and the direction of motion. Work is also defined as the total change of energy of an object.

ercize.

Look at the problem of Bryan and Lucy again, how much work does Bryan exert against the force of gravity if the average force until he reaches the maximum height is 150 N?

Hint: Assume $\theta = 0$ and find s, the distance from the top of the cliff to the maximum height.

Besides regarding work done in the context of force and distance, it is useful to look at work in the context of energy transformations. This change in energy can be gravitational potential energy as in the case of Bryan jumping off the cliff. However, it can also be in the form of kinetic energy, if you exert force over a certain distance, the object will remain in motion if no external forces act upon it. We will come back to work done, defined as the change in energy, in both thermal physics and electrical circuits.

Work done may be defined as a change in energy:

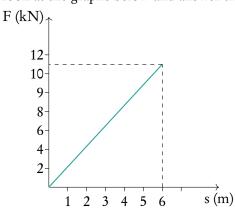
$$W = E_2 - E_1 = \Delta E$$

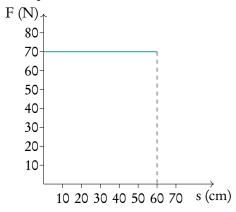


$$W = mgh_2 - mgh = (5)(10)(2-0) = 100 \text{ J}$$

Assuming a frictionless surface, how much work will it take to get a 10 kg ball initially resting to move at $v = 5 \,\text{m/s}$?

Sometimes the IB will ask you to sketch and interpret force-distance graphs. Look at the graphs below and answer the associated questions.





How much work was done on the object shown in the graphs above?

Power as rate of energy transfer & efficiency



Power is typically defined as the energy change over a certain period of time.

$$P = \frac{\Delta E}{\Delta t}$$

$$P = power [Js^{-1}]$$

$$E = energy [J]$$

$$t = time [s]$$

As the change in energy may be defined as work done, we can also write power

$$P = \frac{W}{\Delta t} = \frac{F\Delta s \cos \theta}{\Delta t} = Fv \cos \theta$$

Efficiency is the ratio of useful power coming out of a system to the total power going into the system

$$Efficiency = \frac{useful\ work\ out}{total\ work\ in} = \frac{useful\ power\ out}{total\ work\ in}$$



2.4 Momentum and impulse

2.4.1 Newton's 2 law & force-time graphs

Momentum is what gives the objects their force. One of the most important laws of physics is conservation of momentum; we will see this later in application to collisions.



Momentum is what is used to describe the motion of massive bodies.

Momentum can be defined by re-writing Newton's 2nd law:

$$F = ma = m\frac{\Delta v}{\Delta t} = \frac{\Delta p}{\Delta t}$$

Impulse is the change in momentum of an object.

$$\Delta p = \text{impulse [Ns]}$$

$$F = \text{force [N]}$$

$$t = \text{time [s]}$$

You will often be asked to find the value of Δp from an F vs t diagram.

The law of conservation of momentum says that in any closed system, momentum is always conserved, in other words, momentum is conserved if $F_{\text{ext}} = 0$.

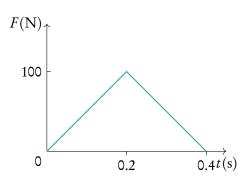
It is good to keep these definitions in the back of your mind, however you will be using the equation below this more often in your calculations.

$$ec{p}=mec{v}$$
 DB



cercize,

Often, problems will ask you about impulse. Here is a problem about someone pushing an object for a very short amount of time, a perfect example of impulse.



What's the maximum force applied to the object?

What's the average force applied to the object?

What's the total change in momentum after the push?

We now return to the concepts of conservation of momentum with the use of collisions as an example.



Elastic collisions energy is conserved.

$$m_1v_1 + m_2v_2 = m_1v_1' + m_2v_2'$$

Inelastic collisions energy isn't conserved.

$$m_1v_1 + m_2v_2 = (m_1 + m_2)v_3$$



THERMAL PHYSICS



	Thermal concepts erature, heat energy, and internal energy – Avogadro
- Temp & the n	. 0,
3.2.	Thermal properties of
matt	
– Therr	nal capacity & specific heat capacity – Phases of matter changes – Latent heat
3.3.	Kinetic model of an ideal
gas	
	nptions of the Kinetic Model – Pressure – State n of an ideal gas



3.1 Thermal concepts

3.1.1 Temperature, heat energy, and internal energy

Upon measuring how hot an object is, we are assuming a dynamic equilibrium in the flow of heat. That is, the net flow of heat between two systems is equal to zero.



Temperature measure of how hot something is (it can be used to work out the direction of the natural flow of thermal energy between two objects in thermal contact) or measure of the average kinetic energy of molecules. It is measured on a defined scale (celsius, kelvin)

$$K = {^{\circ}C} + 273$$

Heat energy transferred from one body to another due to a temperature difference. It is measured in joule (J).

Remember: heat is the transfer of thermal energy. *Heating is a process*, not *a property* (like temperature, pressure, etc.).



Internal energy the sum of all random kinetic energies and mutual potential energies of the particles of the body or system. It is measured in joule (J).

Internal energy does not include the kinetic energy or potential energy of the body as a whole.

An ideal gas has no intermolecular forces, therefore the gas particles have no mutual potential energies therefore the internal energy of an ideal gas depends only on the kinetic energy of the particles (temperature of gas).



Kinetic and potential energies are defined into more specific subgroups of motion and forces.

Kinetic Energy	Potential Energy
Vibrations Rotations Translations	Lattice forces Intermolecular forces

Upon heating or cooling the system, one of two things may happen.

- A change in kinetic energy will change the temperature of the system.
- A change in potential energy will change the phase of the system.

3.1.2 Avogadro & the mole

The mole is used to quantify large amounts of molecules. As we use a dozen to say we have 12 of something, we have a specific variable to say that we have 6.02×10^{23} of something, that is Avogadro's number, $N_A = 6.02 \times 10^{23}$.



Avogadro constant, N_A the number of atoms in exactly 12×10^{-3} kg of the nuclide carbon-12.

Mole amount of substance of a system which contains as many elementary units as there are carbon atoms in 12×10^{-3} kg of carbon-12. The mole is the SI unit for measuring the amount of a substance.

Molar mass the mass of one mole of a substance.



3.2 Thermal properties of matter

3.2.1 Thermal capacity & specific heat capacity

Whenever internal energy is spent on increasing the kinetic energy of a system, the temperature of the system will change. On a microscopic level, a change in temperature is simply an increase in average kinetic energy of the particles that make up the system.



Specific heat capacity, c the amount of energy required to raise the temperature of a unit of mass through 1 K.

Heat (thermal) capacity, C the amount of energy/heat required to raise the temperature of a substance/object through 1 K.

DB

$$Q = mc\Delta I$$
$$Q = C\Delta T$$

Q = heat or amount of energy added [J] $Q = mc\Delta T$ C = thermal capacity C = ther $\begin{array}{c} [kg] \\ [Jkg^{-1}K^{-1}] \end{array}$ $[JK^{-1}]$

Typically, we will be regarding objects or systems with a known mass. In this case, we will have to regard the specific heat capacity.

Phases of matter 3.2.2

To gain a little more intuition into why these phases are so different from one another, we will take a quick look at each of them on a microscopic level.

Phase	Macroscopic	Microscopic
Solid	Volume and shape are approx. constant	Particles held by bonds • Vibrations
Liquid	Volume is approx. constant, shape varies	Weak intermolecular (IM) forces • Translational • Vibrational
Gas	Varying shape and volume	Random motion • Translational • Vibrational



3.2.3 Phase changes



Intermolecular bonds are bonds that hold molecules together due toe forces of attraction.

Phase changes involve the breaking or loosening of intermolecular bonds. When the phase of a body changes, only the potential energy changes, kinetic energy and thus temperature will stay constant. When bonds break, the potential energy of the body increases, as energy is absorbed, and vice versa.

3.2.4 Latent heat

Latent heat is very similar to specific heat capacity except we are not looking at the heat required to change the temperature of a system by a certain amount. Instead we want to know how much heat is needed to change the phase of a certain mass of substance (i.e. melting from solid to liquid).



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Specific latent heat is defined as the amount of heat required to change the state of 1kg of substance.

Specific latent heat

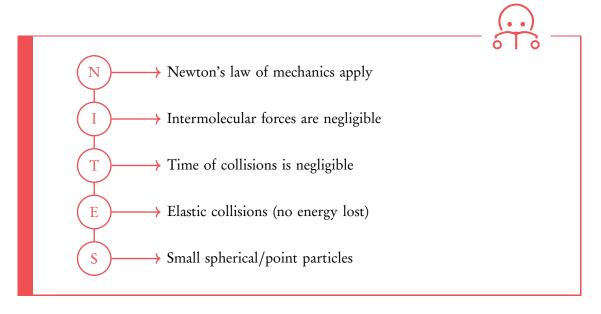
 $L = \text{specific latent heat } [J \, \text{kg}^{-1}]$

Q = mL

3.3 Kinetic model of an ideal gas

3.3.1 Assumptions of the Kinetic Model

There are a few assumptions that should be remembered when dealing with ideal gases; these assumptions can be very easily remembered using the acronym, NITES.



The IB will usually only ask for three assumptions, so if you remember this acronym you have a very high chance of getting full points on any relevant question.

In an ideal gas, temperature is directly proportional to the average kinetic energy of the system.

$$T \propto \frac{mv_{\rm avg}^2}{2}$$

3.3.2 Pressure

Pressure can be looked at in two regimes, the macroscopic and the microscopic regimes.

Macroscopically, pressure is defined as the force exerted over a unit area.

Pressure

$$p = \frac{F}{A}$$

$$P = \text{pressure } [\text{N m}^{-2}] \text{ or } [\text{Pa}]$$

$$F = \text{force } [\text{N}]$$

$$A = \text{area } [\text{m}^2]$$

Microscopically, we consider pressure as the sum of counterforces of all colliding particles with the container over a certain area and between particles themselves.



DB

This involves Newton's third law, as the container in which a gas is held will push back on the particles with an equal and opposite force, enforcing the pressure. If the force of the particles becomes too great for the container to hold, the container will break, as a balloon might if pumped up too large.

3.3.3 State equation of an ideal gas

There is one equation that is very common and useful in thermal physics, the state equation of an ideal gas. A real gas may be approximated by an ideal gas when the density is low. Remember that density is simply $\frac{n}{V}$.

State equation of an ideal gas

 $nR = \frac{PV}{T}$

n = amount of substance [mol] R = ideal gas constant P = pressure V = volume T = temperature [K]

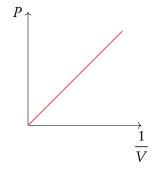
This equation is a direct consequence of the assumptions presented above and the way we have defined pressure. It allows us to relate the various thermodynamic quantities to each other. Expect to be given several of the quantities and making use of this equation in order to calculate the remaining value.

The state equation may be separated into individual proportionality laws that will assist your understanding. These may all be derived from the ideal gas law, when we assume a closed container so that nR does not change.

$$\frac{P_1 V_1}{T_1} = nR = \frac{P_2 V_2}{T_2}$$

At constant temperature $T_1 = T_2$, so that the above becomes $P_1V_1 = P_2V_2$.

The pressure-volume law

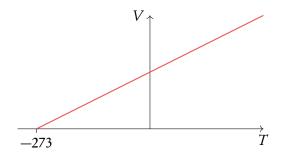


At constant temperature, pressure and volume display inverse proportionality as shown in the diagram.

$$P \propto \frac{1}{V}$$
 or $PV = \text{constant}$

This is also known as Boyle's law.

The volume-temperature law



When measured experimentally in kelvin at constant P, volume and temperature show a linear relationship as as shown in the diagram.

$$\frac{V}{T} = \text{constant}$$

This is also known as Charles' law.

Pressure-temperature relationship

This was similarly found for the pressure-temperature relationship.

$$\frac{P}{T}$$
 = constant

This is known as the Gay-Lussac's law.



OSCILLATIONS & WAVES



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4.1 Kinematics of simple harmonic motion



Displacement (*x*) The amount of distance that an oscillation may be found from equilibrium at an arbitrary point in time.

Amplitude (*A*) The maximum value the oscillation can have.

Period (T) The amount of time it takes to complete a full oscillation.

$$T = \frac{1}{f} = \frac{2\pi}{\omega}$$

Simple harmonic motion (SHM) is oscillatory motion where the resistance force or acceleration is negatively proportional to the displacement.

Conditions of simple harmonic motion:

- Oscillations around an equilibrium point
- Sinusoidal relations between position and time

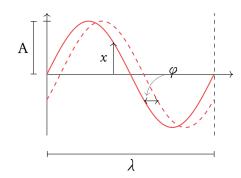


Wavelength (λ) the length of a full period of oscillation.

Angular frequency (ω) The amount of full oscillations per second.

$$\omega = 2\pi f$$

Phase difference (φ) The difference in period between two points in an oscillation



SHM equations:

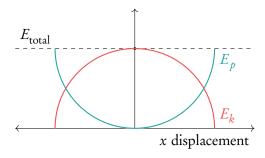
$$F_{\text{res}} = -kx$$
 $ma = -kx$ $a \propto -x$

The solution to this relationship is what we will use in order to solve various problems regarding displacement, velocity and acceleration.



4.2 Energy changes during SHM

Conservation of energy holds in simple harmonic motion. This means that the total energy stays constant and we again have a constant exchange between potential and kinetic energy. It is simpler in oscillations because the total energy in the system is easily defined using the maximum amplitude of the oscillation. The following graph shows the interchange between kinetic and potential energy in the system.



Simple Harmonic Motion(SHM) is described by: $a=-\omega^2 x$. ω is the angular frequency and is related to the period by: $T=\frac{2\pi}{\omega}$

There are two conditions for SHM. Take the mass-spring system as an example.

equilibrium position x = A, t = 0extension x F = -kx $x = 0, t = \frac{T}{4}$ $x = -A, t = \frac{T}{2}$

From this we can deduce that:

$$\omega^2 = \frac{k}{m}$$
 thus,

 $T = 2\pi \sqrt{\frac{m}{k}}$

At small amplitudes the simple pendulum may be approximated as undergoing SHM.

$$\omega^2 = \frac{g}{L}$$

We can calculate velocity at any displacement using: $v = \pm \omega \sqrt{x_0^2 x^2}$.

DB

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4.3 Forced oscillations & resonance

4.3.1 Damping



Damping the process whereby friction causes oscillations to tend back to the equilibrium in real oscillators.

Underdamped there is very little friction; the oscillation goes to zero after several oscillations.

Overdamped a lot of friction; the oscillation never even breaches the equilibrium point and goes slowly to zero without oscillating.

Critically damped this is the optimal amount of friction. For example, car springs are damped so as to go to zero after 1 or 2 oscillations.

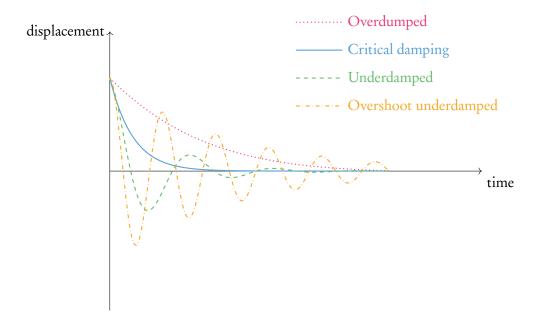


Figure 4.1: Levels of damping



4.3.2 Resonance

The application of an external force may either reinforce or obstruct oscillatory motion. Imagine a father pushing his kid on a swing, if he doesn't time the push exactly as the kid is moving away from him, he will obstruct the oscillation of the swing. This is because every oscillation has a natural frequency associated with it.



Resonance is a phenomenon that the system experiences when the driving frequency approaches the natural frequency.

Natural frequency is defined by the physical limitations of the system.

Driving frequency is the frequency of the external force.

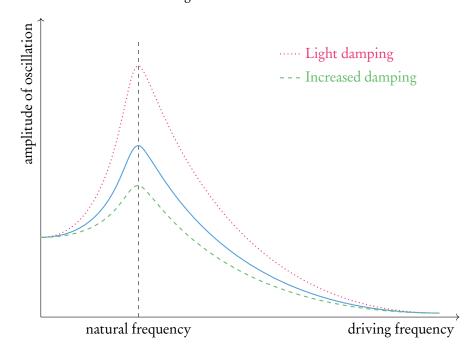


Figure 4.2: Resonance

As the frequency of the external periodic force approaches the natural frequency of oscillation, the effect of resonance on the amplitude of oscillation will increase.



4.4 Wave characteristics

4.4.1 Travelling waves

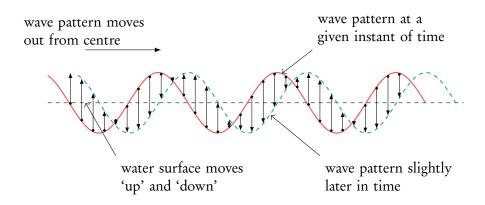


Travelling waves move in space by using the medium they are travelling through to propagate energy. The medium itself is NOT moving in the direction of the wave, it simply oscillates in place due to the energy of the travelling wave.

Transverse waves



Transverse waves are travelling waves in which the direction of oscillation is perpendicular to the direction of energy propagation.



The direction of the wave velocity is the same as the propagation of energy, the wave velocity is given by:

$$v = f \lambda = \left(\frac{s}{t}\right)$$



Longitudinal waves



Longitudinal waves are travelling waves in which the direction of oscillation is parallel to the direction of energy propagation.

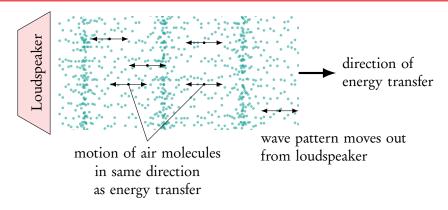
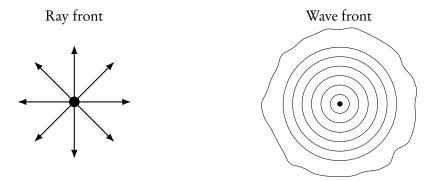
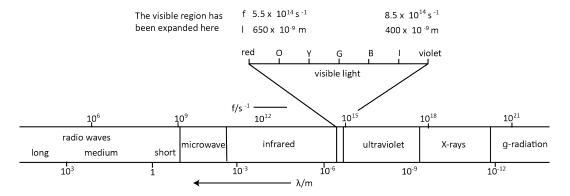


Figure 4.3: Direction of energy flow.



4.4.2 Electromagnetic waves

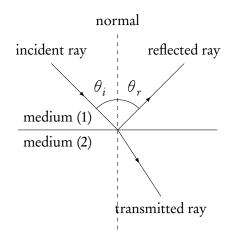
Electromagnetic waves are unique in that they don't need a medium in order to propagate energy. They propagate energy supported by electric and magnetic fields. In the next figure you can see the various important frequency / wavelength / energy ranges of EM waves.





4.5 Wave properties

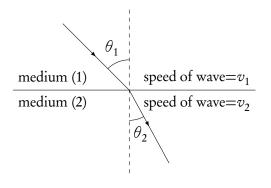
Reflection



Imagine for example, a ray of light being reflected off water or a mirror. This phenomenon is rather intuitive in that the incident angle θ_i is equal to the angle of reflection θ_r .

$$\theta_i = \theta_r$$

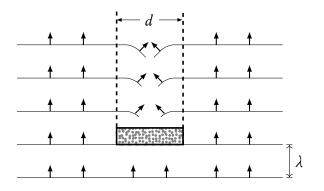
Refraction



Important to remember is that as a ray enters a medium with a different refractive index, the wavelength and velocity will change and the frequency will remain constant.

$$\frac{\sin \theta_1}{\sin \theta_2} = \frac{n_2}{n_1} = \frac{v_1}{v_2}$$

Diffraction



For diffraction to occur, the disturbance must be of the *same* order of magnitude as the wavelength. Furthermore, as the wave is diffracted, the wavelength does *not* change, nor does the frequency or velocity.

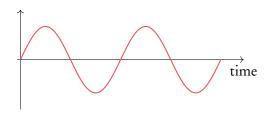


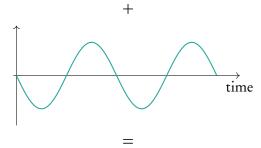
Interference

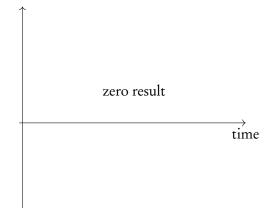
In all problems encountered within the IB, the sources of the waves are coherent, this means that they have the same wavelength. When the waves add up, they undergo constructive interference; when they subtract, they undergo destructive interference.

Destructive interference

$$\left(n + \frac{1}{2}\right)\lambda = \text{path difference}$$

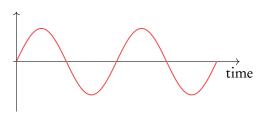


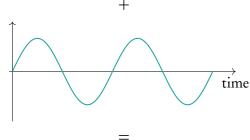


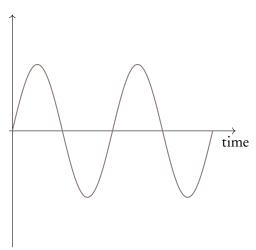


Constructive interference

 $n\lambda$ = path difference







4.6 Standing waves

Imagine plucking the string of a guitar. What does the string do? It vibrates back and forth, at a certain frequency. Now if we put our finger right on the center of the string, this point will not be allowed to vibrate and the result is that the two ends will be vibrating back and forth inversely to one another. This is shown in the Figure 4.4.

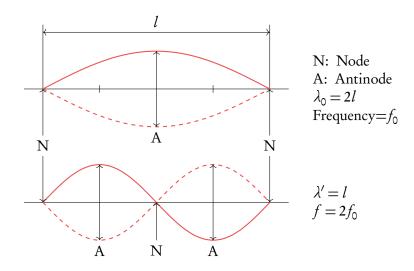


Standing wave is a wave in a medium in which each point on the axis of the wave has an associated constant amplitude.

A node is a point on the standing wave that does not oscillate.

An antinode is a point on the standing wave that is always oscillating to the maximum amplitude.

Figure 4.4: Vibrating guitar string.



There are several notable differences between standing waves and travelling waves:

Standing

- Energy is stored
- Maximum amplitude depends on position
- All points between nodes have equal phase

Travelling

- Energy is transmitted
- Maximum amplitude is universal

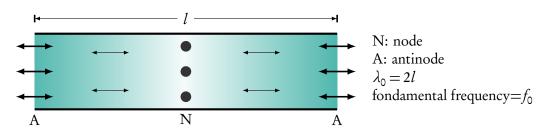


When solving problems involving standing waves, we will focus on:

- The length of the wave, *L*
- Its wavelength, λ
- Its harmonic frequencies, f

It is important to know the various boundary conditions that may lead to standing waves. Above we already gave the example of a fixed string, however, in the IB you should also be aware of the various systems set up in pipes.

Figure 4.5: Open pipe.



Every standing wave has a fundamental frequency corresponding to the most simple oscillation, for a system open at both ends the fundamental frequency is calculated by way of fundamental wavelength:

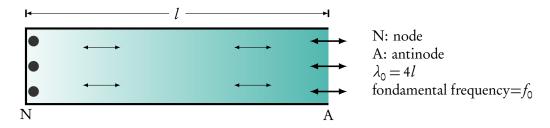
$$\lambda_0 = 2L$$

where λ_0 is the fundamental wavelength and L is the length of the standing wave. To calculate the rest of the harmonic wavelength or frequencies we use the relation:

$$2L = n\lambda$$

In both instances we may use $f = \frac{v}{\lambda}$ to calculate the corresponding frequency.

Figure 4.6: Half open pipe.



For a system closed at one end, the fundamental wavelength may be calculated using:

$$2L = \left(n - \frac{1}{2}\right)\lambda$$



This added factor of $\frac{1}{2}$ can be accounted for by the half-wavelength phase difference that occurs in a closed system, that is, there is a node at the closed end of the wave and an antinode at the open end. This equation may be used specifically to calculate the harmonic frequencies in a one-end open pipe.



ELECTRICITY AND MAGNETISM



5.1 Electric fields and potential

5.1.1 Charge

There are two types of charge, positive and negative, and they are the opposite of each other. Like charges repel each other while opposite charges attract.



Electric charge physical property of matter that causes it to experience a force to other electrically charged matter

Conservation of charge just like energy, electric charges are conserved in all physical processes

The SI derived unit of electric charge is the coulomb (C). Coulomb's law quantifies the force between two particles, which depends on the amount of charge and the distance between them.

Coulomb's law: force between charges

$$F = k_e \frac{q_1 q_2}{r^2}$$

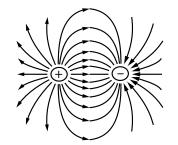
$$F = k_e \frac{q_1 q_2}{r^2}$$

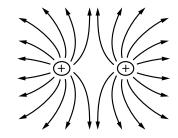
$$k_e = \text{Coulomb's constant } 8.99 \times 10^9 \,\text{N m}^2 \,\text{C}^{-2}$$

$$q_1 = \text{charge} \qquad [\text{C}]$$

$$q_2 = \text{charge} \qquad [\text{C}]$$

$$r = \text{distance} \qquad [\text{m}]$$







5.1.2 Nature of electric fields

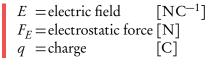
Electric field is the electrostatic force on a stationary test particle of unit charge 1 C

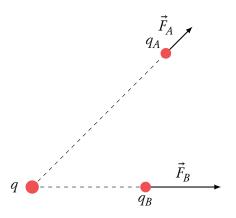
Electric fields are caused by electric charges, and the electric field strength diminishes further away from its source.

Inside an electric field of a particular strength, the force exerted on a test charge depends *only* on the amount of charge.

The electric field strength is defined as the electrostatic force per unit charge.

$$E = \frac{F_E}{q}$$





- particle q_A that is further away from q will experience a smaller force \vec{F}_A ,
- particle q_B that is closer to q which will experience a larger force \vec{F}_B

5.1.3 Potential difference

Since charge inside an electric field experience a force, moving a test particle requires work that changes its *electric potential energy*.



Voltage = electric potential difference ΔV the difference in electric potential energy of a charge that *moves* between two points *per* unit charge $[V = JC^{-1}]$

When some unknown amount of charge moves in an electric field, its potential difference changes. (much like when we lift an apple of unknown weight from the ground) The amount of electric potential difference depends on the strength of the electric field, and the distance the charge moved:



Note that test charges are always *positive*,

unless the question

an electron)

states otherwise (e.g.

Electric potential difference by moving a charge in an electric field:

$$\Delta V = E \cdot \Delta x$$

$$V = \text{electric potential difference [V]}$$

$$E = \text{electric field}$$

$$x = \text{distance}$$

$$[V]$$

$$E = \text{electric field}$$

$$E = \text{electric field}$$

$$E = \text{electric field}$$

$$E = \text{electric field}$$

The electric potential difference ΔV is independent of the charge, since the value is *per* unit charge, so that once the charge is known the amount of energy (work) can be calculated.

Work done by moving a charge in an electric field:

$$W = \Delta V \cdot q$$
 (5.2) $W = \text{work}$ [J] $V = \text{electric potential difference [V]}$ $q = \text{charge}$ [C]

Since the amount of work done on an electron by a potential difference is very small, since the charge of the electron is very small, eV units are often used instead of J.



Electron volt eV: 1.602×10^{-19} J is the amount of work needed to change the electric potential of an electron by 1 V. It is a unit of energy!

5.2 Electric current



Electric current [A] the flow of electric charge, the amount of charge that flows per unit time

$$I = \frac{\Delta q}{\Delta t}$$
 $I = \text{current [A]}$ $q = \text{charge [C]}$ $t = \text{time [s]}$

5.2.1 Direct current (dc)

While positive metal nuclei in metals are held in place and can only vibrate, electrons in a metal can move freely from one metal nuclei to another. The 'sea of electrons' are at all times homogeneously distributed throughout the metal, ensuring that the positive charge of the metal nuclei are at all times neutralised. When a potential difference across the metal is applied, electrons accelerate in the externally applied electric field proportional to the maginitude of that field. Because electrons bump into the a.o. metal



nuclei, transferring some energy in the collision thus heating up the metal because the nuclei will vibrate more, the electrons attain a specific average velocity proportional to the electric field.

Drift velocity the average velocity of electrons in a material due to an electric field

More electrons per unit time will move [A]: 1. when a higher potential difference is applied [V], 2. when electrons can move through the material more easily and 3. the cross-section of the material is larger. 2 & 3 together $[\Omega]$

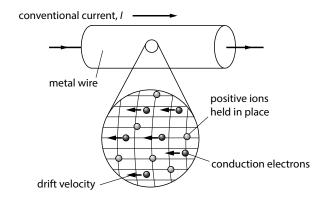
Ohm's Law

$$R = \frac{V}{I}$$

$$R = \text{resistance } [\Omega]$$

$$V = \text{voltage } [V]$$

$$I = \text{current } [A]$$



Resistance of a wire from material properties

$$\rho = \frac{RA}{L}$$

which after rewriting gives

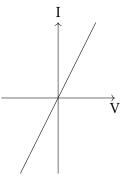
$$R = \rho \frac{L}{A}$$

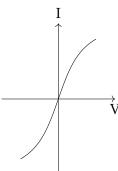
$$ho =$$
 resistivity of the material $[\Omega \, \mathrm{m}]$ $L =$ length of the wire $[\mathrm{m}]$ $A =$ cross-sectional area of the wire $[\mathrm{m}^2]$

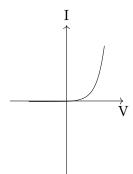




A device is ohmic if current and voltage are proportional, because resistance is constant at all values for current and voltage. When they are not proportional, the system is said to be non-ohmic.







- (a) metal at constant T (ohmic)
- (b) filament lamp (non-ohmic)
- (c) diode (non-ohmic)

5.2.2 Power dissipation

Power dissipation resistance to electric current causes a material to warm up (when the electrons bounce off positive ions)

The power input/output of a system is the amount of energy per second that it uses/produces. Your laptop consumes a particular amount of energy per second [J s⁻¹], which is expressed in watts [W].

Power of electrical devices

$$\frac{\Delta E}{\Delta t} = P = VI$$

 $\frac{\Delta E}{\Delta t} = P = VI$ substituting Ohm's law into V or I gives

$$P = \text{power}$$
 [W]=[J s⁻¹]
 $V = \text{potential difference}$ [V]
 $I = \text{current}$ [A]

$$P = I^2 R = \frac{V^2}{R}$$

While we often consider devices are power consumers, wires also consume power due to the resisivity of the material. To calculate the amount of electrical energy that is converted into heat by a wire, the above formula is often used in the form of $P = I^2R$. This formula also shows that powerloss in a wire is independent of the voltage!



5.2.3 Electromotive force



Electromotive force (e.m.f.) is the largest potential difference that may be experienced by charges moving around the circuit.

Note that the e.m.f. or $\mathscr E$ is equivalent to $V_{\rm tot}$ or the potential difference across the circuit.

The battery that is providing the driving force of the circuit often has some form of internal resistance r. It is calculated by using the current I and the electromotive force $\mathscr E$ of the circuit, calculated using the following formula.

Electromotive force

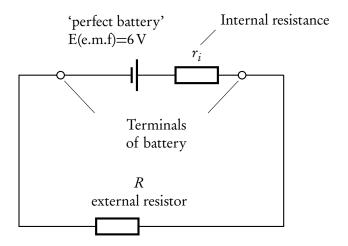
$$\mathcal{E} = I(R+r)$$

$$I = \text{current} \qquad [A]$$

$$R = \text{external resistance} \qquad [\Omega]$$

$$r = \text{internal resistance} \qquad [\Omega]$$

Figure 5.1



$$\begin{aligned} \text{e.m.f.} &= I \times R_{total} \\ &= I(r_i + R) \\ &= Ir_i + IR \\ \underbrace{IR}_{\text{terminal p.d.},V} &= \text{e.m.f.} - \underbrace{Ir_i}_{\text{'lost' volts}} \end{aligned}$$



5.3 Electric circuits

5.3.1 Resistors

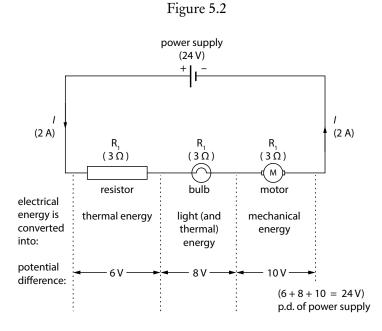


Resistors in series

• The potential difference is split between the resistors. That is, they may be summed linearly

$$V_{\text{tot}} = V_1 + V_2 + V_3 R_{\text{tot}} = R_1 + R_2 + R_3$$

• Current is constant throughout all resistors.



A variable resistor divides the potential difference accross it. The easiest way of looking at these is to consider two resistors in series: the potential difference is split between the resistors. When the resistance of these changes, so does the potential difference: so using the variable resistor we can vary the potential difference.

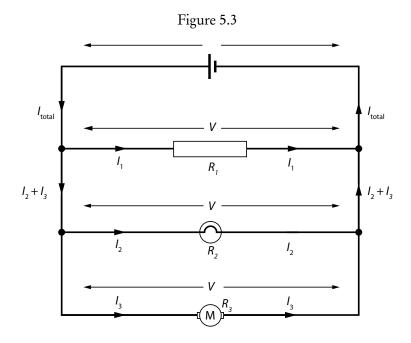




Resistors in parallel

- The potential difference is the same across all resistors in parallel.
- The current varies per resistor depending on the amount of resistance.

$$\frac{1}{R_{\text{tot}}} = \frac{1}{R_1} + \frac{1}{R_2}$$
$$I_{\text{tot}} = I_1 + I_2$$





5.3.2 Electrical meters



Ammeter is a current-measuring meter. It needs to be connected in *series* at the point where the current is to be measured. An ideal ammeter would have zero resistance

Voltmeter is a meter that measures potential difference. It needs to be placed in *parallel* with the component or components being considered. An ideal voltmeter has infinite resistance.

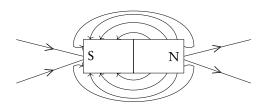
5.4 Magnetic fields

	E - electric	B - magnetic
Caused & affected by:	charges	magnets (or currents)
Two types:	positive and negative charge	north and south pole
Force rule:	like charges repel like charges attract	like poles repel like poles attract

Magnetic fields may be induced by the movement of charge.

Figure 5.4





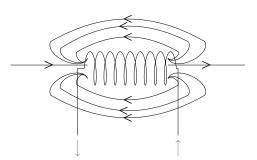


Figure 5.6



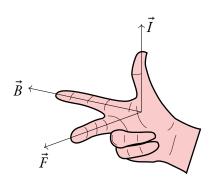
Right-hand rule

$$Middle = F$$
 (force)

Pointer = B (magnetic field)

Thumb = I (current)

FBI



This rule is used whenever you are solving problems using either:

$$F = q v B \sin \theta$$

(moving charge)

$$F = BIL \sin \theta$$

(current in a wire)

An electron approaches a bar magnet as shown in the figure. If $v = 5.000 \,\text{m/s}$, $B = 5 \,\text{T}$.



- 1. Draw the field lines in the diagram.
- 2. Draw the direction of the force on the electron.



3. What is the magnitude of this force?

Using the equal and opposite forces of two current carrying wires on each other, we can define the ampere.



The ampere is defined through the magnetic force between two parallel wires. If the force on a 1 m length of two wires that are 1 m apart and carrying equal currents is 2×10^{-7} N, then the current in each wire is defined to be 1 A.



CIRCULAR MOTION AND GRAVITATION



6.1.	. Circular motion
6.2.	. Gravitational field
• • • • • • • • • • • • • • • • • • • •	ewton's universal law of gravitation – Gravitational field



6.1 Circular motion

Circular motion is common in everyday life. An interesting example is the motion of planets around the Sun in nearly circular orbits. The pre-requisite for circular motion is a force directed towards the centre, a centripetal force.

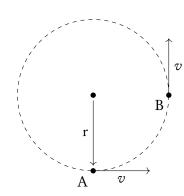


Centripetal acceleration A body moving along a circle of radius R with speed v experiences centripetal acceleration given by

$$a = \frac{v^2}{r}$$

and is directed towards the centre.

xample.



- a) Draw the force vector at point A & B.
- b) Draw the direction of the net force as the object moves from point A → B,

ercize.

- 1. A car is on a racing track and wants to take a hair-pin needle corner as fast as possible. The driver happens to know that the tires can exert a maximum friction force of 20.000 kN.
- 2. Assuming a hemispherical hairpin corner with r = 20 m, what is the maximum velocity with which a 500 kg race car can take the corner?
- 3. There's an even tighter corner right after the last one with r = 15 m. If they want to maintain the same velocity how much mass should be removed from the car?



6.2 Gravitational field

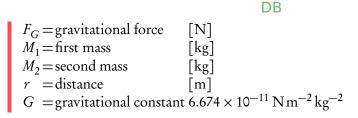
We have briefly discussed gravity in mechanics, in the context of the acceleration we feel on Earth. However, as Newton famously pointed out in his glory days, gravity may be generalized to encompass the entire universe. This is why it has been coined Newton's universal law of gravitation. Although Einstein accounted for high-energy anomalies, this law still holds strongly when discussing non-relativistic scenarios.

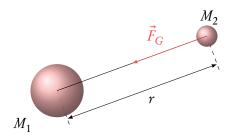
6.2.1 Newton's universal law of gravitation

Newton's universal law of gravitation:

$$F_G = G \frac{M_1 M_2}{r^2}$$

- Gravitational force is always attractive.
- It is only *significant* for very massive objects (i.e. planets and stars).
- Spheres can be treated as point particles because the center of mass is located at the center.





6.2.2 Gravitational field strength

The gravitational field strength, g, is the value we use to define acceleration due to gravity.

The gravitational field is defined as the force due to gravity per unit mass.

$$g = \frac{F_G}{m} = G\frac{M}{r^2}$$

$$g = \text{acceleration} \quad [\text{m s}^{-2}]$$

$$G = \text{gravitational constant } 6.674 \times 10^{-11} \, \text{N m}^{-2} \, \text{kg}^{-2}$$

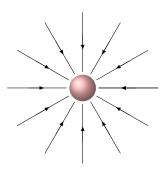
$$M = \text{mass} \quad [\text{kg}]$$

$$r = \text{distance} \quad [\text{m}]$$

In mechanics, we use the correct value for Earth, $\approx 9.81\,\mathrm{m\,s^{-2}}$. However, the gravitational field strength can be easily derived from the law of gravitation.



Field diagrams are used when describing all three kinds of fields mentioned earlier (electric, magnetic & gravity), for gravitational fields these are the most straightforward as gravity will only attract other massive objects. The field will always point the way that any massive object moves.



ercize.

Now try drawing the field lines for these massive objects:





6.2.3 Similarities between gravitational and electrostatic fields

Electrostatic fields behave nearly analogous to gravitational fields.

Newton's law

Coulomb's law

$$F_G = G \frac{M_1 M_2}{r^2}$$

$$F_E = k \frac{q_1 q_2}{r^2}$$

- We assume the use of point charges.
- Forces act along the connection between the two points.
- Both gravitational and electrostatic forces are additive.
- Both fields are proportional to the inverse of the square of the distance.

The main difference that must be taken into account is that electric charge may be either positive or negative. It follows that opposite charges will attract but like charges will repel, while the gravitational force is always attractive.



ATOMIC AND NUCLEAR PHYSICS



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7.1 Atomic structure

Atoms differ in how many protons, neutrons, and electrons they have. These apparently small differences do make it impossible for us to have such a wide variety of materials.

7.1.1 Atomic models



Plum pudding model protons, neutrons and electrons are homogeneously distributed in the atom

Rutherford model protons and neutrons reside in a small and dense nucleus, electrons are homogeneously distributed

Bohr model protons and neutrons reside in a small and dense nucleus, electrons reside in atomic orbitals around the nucleus (electron cloud)

Subatomic particles

Mass	Relative mass	Charge	Relative charge	Notation
$1.67 \times 10^{-24} \text{ g}$ $1.67 \times 10^{-24} \text{ g}$		$1.60 \times 10^{-19} \mathrm{C}$	+1 0	p ⁺
$9.11 \times 10^{-28} \mathrm{g}$	U		— 1	e ⁻

Proof of a small, dense and positively charged nucleus

In the Rutherford experiment a beam of α particles was directed at a thin metal foil and the scattering pattern was measured by using a fluorescent screen. Thomson's model of the atom incorrectly predicted the alpha particles to go straight through the foil, instead a fraction of the particles were scattered (forced to deviate from a straight trajectory) by:

- Electrostatic repelling force between positive α particle and positive metal nuclei proved that the positive charge was concentrated
- A small number of collisions with metal nuclei caused a deflection of over 90°, proving that the metal nuclei were dense and confined to a region of linear size approximately equal to 10⁻¹⁵ m.



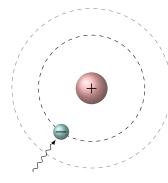
7.1.2 Emission and absorption spectra

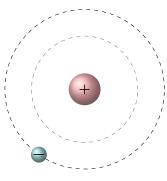
Electrons in atoms can have very particular (discrete) amounts of energy, this means that the energy levels of electrons are quantized. Electrons can absorb and emit energy in various ways, one is way is in the form of absorbing and emitting photons.

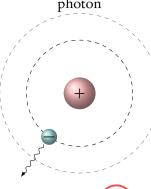
Electron in ground state absorbs a photon

Energized electron jumps to a wider orbit

Electron returns to its ground state, emitting a photon









Discrete light quantum the amount of photon energy absorbed/emitted, equal to the energy difference of two electron energy levels

$$E = hf = \frac{hc}{\lambda}$$

E = energy

h = Planck's constant

f = frequency

c =speed of light

 $\lambda =$ wavelength

Emission



Emission an electron can emit a photon with a particular amount of energy, the electron will be in a lower 'excited energy state' or in the 'groundstate'

Atoms with electrons in the excited energy state emit light by 'falling down' to lower energy levels. The energy of the photon emitted equals the energy difference of two electron energy levels. When such emission light is passed through a prism emission lines are observed, each line represents the energy difference between two electron energy levels.



Figure 7.1: Emission spectrography setup.

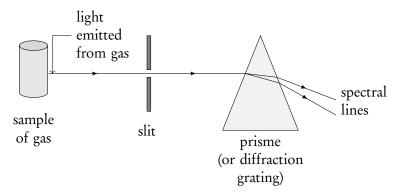
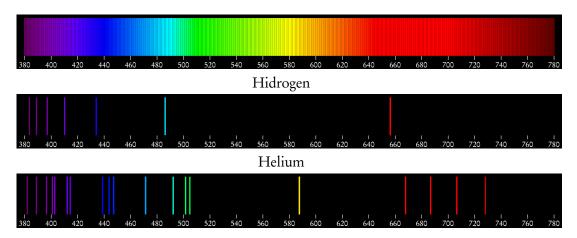


Figure 7.2: Emission spectrum



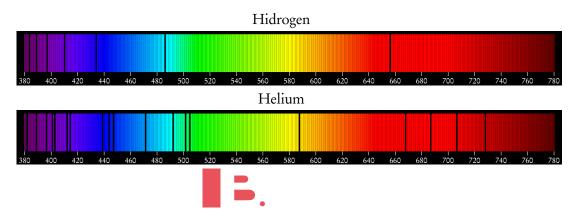
Absorption



Absorption an electron can absorb a photon with a particular amount of energy, the electron will be in a higher 'excited energy state'

When white light is passed through a sample with gaseous atoms, photons with energy equal to the energy difference of two electron levels can be absorbed. The remaining light is then passed through a prism, resulting in a spectrum wherein light of particular wavelength is absent.

Figure 7.3: Absorption spectrum



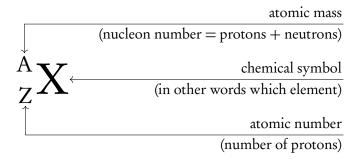
ACADEMY

7.2 Nuclear structure



Nucleon is either a neutron or a proton.

Nuclide is a nucleus that contains a specified number of protons and a specified number of neutrons.



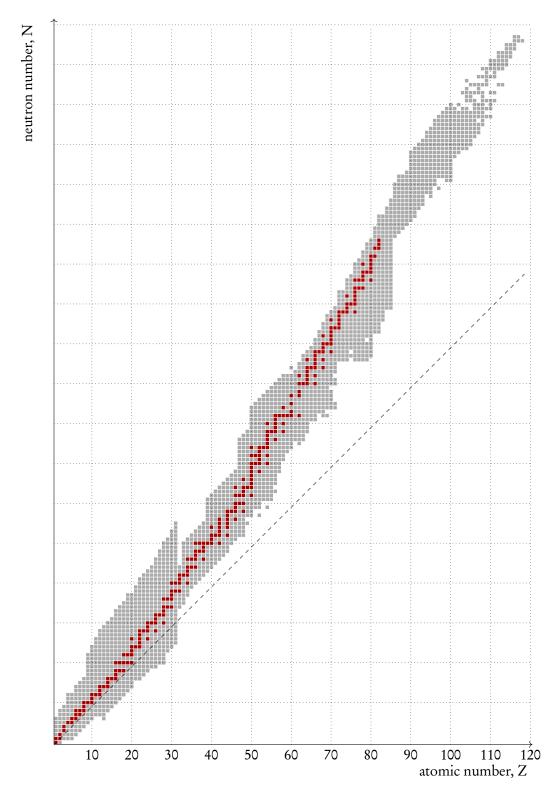
Isotopes a species of an atom that contains a specified number of protons and a specified number of neutrons (like a nuclide), and electrons. While the term isotope refers to the entire atom (including electrons), nuclide refers to only the nucleus.

Since all protons are in the nucleus, and like charges repel, there must be a force that holds the protons together and prevents them from falling apart. This force is called the strong nuclear force, and there are a few phenomena that we know this must adhere to:

- It must be strong, as the gravitational attraction is not nearly enough to overcome the electrostatic force that is repelling the protons from each other.
- As the force cannot be observed anywhere other than within the nucleus, it must act on a very short range
- It is likely to involve neutrons as well. Small nuclei tend to have equal number of
 protons and neutrons. Large nuclei need proportionally more neutrons in order to
 remain stable.



The graph below shows the relationship between the atomic number and the number of neutrons in a range of elements.





7.3 Radioactivity



Radioactive decay when an unstable nucleus emits a particle (alpha α , beta β , gamma γ).

- Note that radioactive decay is both a random and spontaneous process.
- Note that the rate of radioactive decay decreases exponentially with time.
- Note that radiation that originates from the atom is often the result of electron transitions. These do not fall under the definition of radioactivity.

Alpha decay when a chunk of the nucleus of an unstable atom is emitted in the form of a helium nucleus ⁴₂He²⁺. What is left of the atom will have to be such that the protons and neutrons balance on each side of the equation.

$${}_{Z}^{A}X \longrightarrow {}_{(Z-2)}^{(A-4)}Y + {}_{2}^{4}\alpha$$

Beta decay, $_{-1}^{0}\beta$ or $_{-1}^{0}e^{-}$ occurs when a neutron in an unstable atom breaks up into a proton and an electron, of which the electron is then emitted along with an antineutrino.

$$_{0}^{1}$$
n $\longrightarrow _{1}^{1}$ p $+ _{-1}^{0}\beta + \overline{\nu}$

such that

$${}_{Z}^{A}X \longrightarrow {}_{Z+1}^{A}A + {}_{-1}^{0}\beta + \overline{\nu}$$

Gamma decay ${}^0_0 \gamma$ is somewhat different from the other types of radiation in that they are part of the electromagnetic spectrum. After their emission, the nucleus has less energy but its mass number and its atomic number have not changed. It is said to have changed from an exited state to a lower energy state.

$${}_Z^AX^* \longrightarrow {}_Z^AX + {}_0^0\gamma$$

Effects of radiation

All three types of radiation are *ionizing*. This means that as they go through a substance, collisions occur which cause electrons to be removed from atoms, forming ions. When ionization occurs in biologically important molecules, such a DNA, it could cause cells to stop working or multiplying, or even become malignant or harm other cells. If this process perseveres, the group of malignant cells together forms what we call cancer.

Property	Alpha (α)	Beta (β)	Gamma (γ)
Effect on photographic film	Yes	Yes	Yes
Penetration ability	Low	Medium	High
Typical material needed to absorb it	10 ⁻² mm aluminum; paper	A few mm aluminum	10 cm lead
Approximate number of ion pairs produced in air	10 ⁴ per mm travelled	10 ² per mm travelled	1 per mm traveled
Typical path length in air	A few cm	Less than one m	Effectively infinite
Deflection by E and B fields	Behaves like a positive charge	Behaves like a negative charge	Not deflected
Speed	$\approx 10^7 \mathrm{ms^{-1}}$	$\approx 10^8 \text{m s}^{-1}$, highly variable	$3 \times 10^8 \mathrm{m s^{-1}}$ (speed of light)

Half-life

Radioactive decay of a single specific nucleus is not predictable since it is a random process, we can only know the chance of a decay occurring within a period of time. The decay rate of a sample is proportional to the number of atoms in the sample, which means that radioactive decay is an exponential process.

The number of atoms of a certain element, N, decreases exponentially over time. Mathematically this is expressed as:

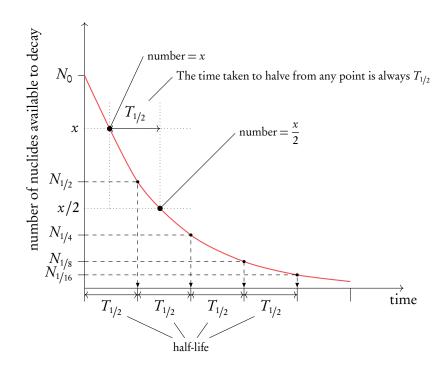
$$\frac{\mathrm{d}N}{\mathrm{d}t} \propto -N$$

In the graph shown below, the time taken for half the number of nuclides to decay is always the same, whatever starting value we choose. This allows us to express the chances of decay happening in a property called half-life, $T_{1/2}$.



Radioactive half-life the time taken for half the number of radioactive nuclei in a sample to decay. Half-lives can vary from fractions of a second to millions of years.





Note that if the half-life of a nuclide is 3 days, the whole sample will not be decayed in 6 days, but rather half a half will remain, that is a quarter.



7.4 Nuclear reactions



Artificial (induced) transmutation when a nucleus is bombarded with a nucleon, an alpha particle or another small nucleus, a nuclear reaction is initiated resulting in a nuclide with a different proton number (a different element)

First, the target nucleus 'captures' the incoming particle and then an emission takes place.

$${}_{2}^{4}\text{He}_{2} + {}_{7}^{14}\text{N} \longrightarrow {}_{8}^{17}\text{O} + {}_{1}^{1}\text{p}$$

The individual masses involved in nuclear reactions are tiny ($\sim 10^{-27}$ kg), so in order to compare atomic masses, physicists often use unified mass units, u.



Unified Atomic Mass Unit $\frac{1}{12}$ the mass of Carbon-12, approximately equal to the mass of 1 proton / 1 neutron

Mass defect



Mass defect is the difference between the total mass of the nucleus and the sum of the masses of its individual nucleons

Bringing protons together in a nucleus requires work to overcome the electrostatic repelling force, while together with neutrons strong nuclear forces form that release energy. The strong nuclear forces that bond protons and neutrons is larger than the electrostatic repelling force, so there is a net release of energy. Conservation laws state that this energy must come from somewhere: Einstein's famous mass-energy equivalence relationship.

$$E = mc^{2}$$

$$E = energy [J]$$

$$m = mass [kg]$$

$$c = speed of light [m s-1]$$

1 kg of mass is equivalent to 9×10^{16} J of energy, which is a huge amount of energy. At the atomic scale the electronvolt (eV) is typically used instead of joule (J).



$$1 \text{ eV} = 1.6 \times 10^{-19} \text{ J}$$

 $1 \text{ MeV} = 1.6 \times 10^{-13} \text{ J}$

1 u of mass converts into 931.5 MeV

Mass defect calculations are very delicate given the long decimals, don't be intimidated by this and simply approach the question carefully and precisely.

	Mass defect			
	Information given: • Atomic mass of carbon-14 = 14.0003	 Atomic mass of carbon-14 = 14.000 324 2 u; Atomic mass of nitrogen-14 = 14.003 074 u; 		
1.	Find mass on both sides of equation	Mass of LHS = nuclear mass of carbon-14 14.003242 - 6(0.000549) = 13.999948 Mass of RHS = nuclear mass of nitrogen-14 + mass of 1 e ⁻ 14.003242 - 7(0.000549) + 0.000549 = 13.999780		
2.	Find the mass difference	Mass difference = mass of LHS - mass of RHS $13.999948 - 13.999780 = 0.000168$		
3.	Convert to $\frac{J}{mol}$	Energy released per decay $0.000168\mathrm{u} \times 931.5\mathrm{MeV}\mathrm{u}^{-1}$ $= 0.156492\mathrm{MeV}$ $14\mathrm{g}$ of carbon-14 means 1 mol (6.02×10^{23}) decays $0.156592\mathrm{MeV} \times 6.02\times10^{23}$ $= 9.424\times10^{22}\mathrm{MeV}$ $9.424\times10^{22}\mathrm{MeV} \times 16\times10^{-13}$ $= 15.142\mathrm{J}$		

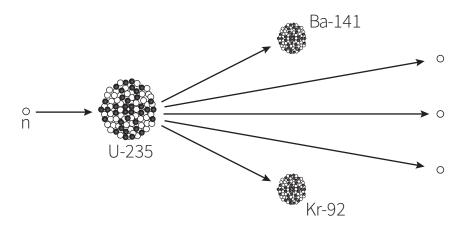


7.5 Fission, fusion, and antimatter

7.5.1 Fission



Fission the nuclear reaction whereby a heavy nucleus splits into two smaller nuclei of roughly equal mass, elements heavier than iron release of energy



It is the reaction that is used in nuclear reactors and atomic bombs. A typical single reaction might involve bombarding a uranium nucleus with a neutron. This can cause the uranium nucleus to break up into two smaller nuclei. Only one neutron is needed to initiate the reaction while three are released. Each neutron can continue causing another reaction; this is called a chain reaction.

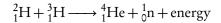
$$_{0}^{1}n + {}^{235}_{92}U \longrightarrow {}^{141}_{56}Ba + {}^{92}_{36}Kr + 3 \, {}^{1}_{0}n + energy$$

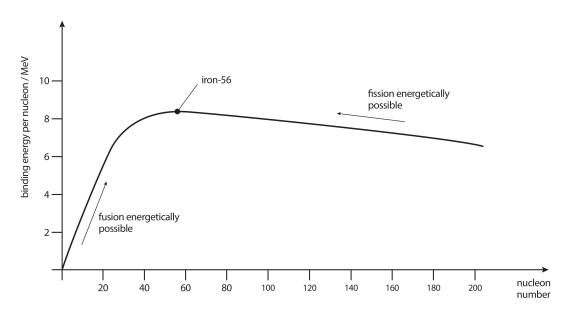


7.5.2 Fusion



Fusion two nuclei 'fuse' to form one larger nuclei, when elements up to iron are formed energy is released in the process. This is the process that fuels stars.





Whenever a nuclear reaction (fission or fusion) releases energy, the products of the reaction are in a lower energy state than the reactants. Loss of mass must be the source of this energy. In order to compare the energy states of different nuclei, physicists calculate the binding energy per nucleon.

- Binding Energy: energy released when a nuclide is assembled from its individual components. Or, the energy required when the nucleus is separated into its individual components.
- Binding Energy per Nucleon: energy released per nucleon when a nuclide is assembled from its individual components. Or, the energy required per nucleon when the nucleus is separated into its individual components.
- The nucleus with the largest binding energy per nucleon is Iron-56 (shown in the graph above on the highest point). A reaction is energetically feasible if the products of the reaction have a greater binding energy per nucleon than the reactants.



7.5.3 Antimatter

The nuclear model given in the previous pages is somewhat simplified. One important component of the nuclear model that has not been mentioned is antimatter



Antimatter every form of matter has an equivalent form of antimatter.

When matter and antimatter come together, they annihilate each other, this occurs in particle colliders.

Another form of radioactive decay that may take place is v^+ or positron decay. A proton decays into a neutron and the antimatter version of an electron, a positron, is emitted.

$${}_{1}^{1}p \longrightarrow {}_{0}^{1}n + {}_{+1}^{0}\beta^{+} + \nu$$

$${}_{10}^{19}Ne \longrightarrow {}_{9}^{19}F + {}_{+1}^{0}\beta^{+} + \nu$$

7.6 Elementary particles

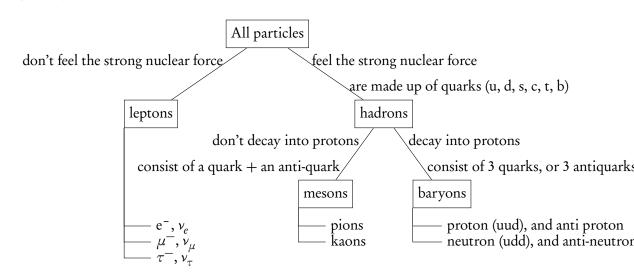
7.6.1 Quarks, leptons and exchange particles



Elementary particle is a particle that is not made out of any smaller component particles

Note that protons and neutrons are subatomic, not elementary particles

These are the three classes of elementary particles: quarks, leptons and exchange particles (bosons).





7.6.2 Quarks – strong nuclear forces

Quark flavour		Charge Q	Baryon number B	Strangeness S
Up	u	+2/3e	+1/3	0
Down	d	-1/3e	+1/3	0
Strange	S	-1/3e	+1/3	— 1
Charm	c	+2/3e	+1/3	0
Bottom	b	-1/3e	+1/3	0
Top	t	+2/3e	+1/3	0

Each quark has an associated anti-quark which has the same mass, but opposite electric charge and baryon number. So while each quark has baryon number of $+\frac{1}{3}$, and each anti-quark a baryon number of $-\frac{1}{3}$, the baryon number B of the combined particle is the sum of the baryon numbers of the individual quarks.

3 quarks combine to form baryons (B=1) 1 quarks and 1 anti-quark form mesons (B=0) Proton p+: uud - TUO-Door = two up one down from u/anti-u and d/anti-d quarks Neutron n0: udd - OUT-Door = one up two down

Isolating a single quark is impossible, it would require infinite energy.

7.6.3 Leptons – weak nuclear forces

There are 6 types of leptons: electron and its neutrino, muon and its neutrino, tau and its neutrino. Tau is the heaviest, then muon, the electron is the lightest. Leptons interact with the weak nuclear interactions, and those with electric charge also interact with the electromagnetic interaction.

Leptons are assigned a quantum number called a family lepton number: L_e , L_{μ} , L_{τ} . The table below shows the various leptons and their properties. Again, take into account that anti leptons have opposite properties except their mass.

Leptons are *not* made of quarks



Lepton	L_e	L_{μ}	$L_{ au}$
e ⁻	+1	0	0
ν_e	+1	0	0
μ^-	0	+1	0
$ u_{\mu}$	0	+1	0
$\dot{ au}$	0	0	+1
$ u_{ au}$	0	0	+1

7.6.4 Bosons = exchange particles

Summarizing the elementary particles up to now in a table we have 6 quarks, 6 leptons and apparently 4 more exchange particles that represent the interactions or forces between those. For example, electrostatic interactions are mitigated by photons = γ , the strong nuclear force by gluons = g, and the weak nuclear force by $Z^0/W^+/W^-$ exchange particles.

Gravity and the Higgs boson are ignored here

				Exchange particles	Interaction
Quarks	u	c	t	γ	EM
	d	S	b	g	SN
Leptons	e-	μ^{-}	$ au^-$	Z	WN
	v_e	$ u_{\mu}$	$ u_{ au}$	W^{\pm}	WN

The mass of the exchange particle and the range of the interaction are inversely proportional, so while a photon has no mass it has infinite range. When two electrons are repelled due to their similar charges a (virtual) photon is responsible to carry this repelling interaction. These interactions can be shown in Feynman diagrams.

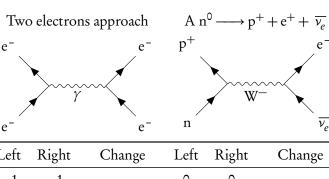
7.6.5 Feynman diagrams

Rules for Feynmann diagrams:

- y-axis: Originating particles start at the bottom, produced particles point upwards
- *x*-axis: Exchange particles change the nature or direction of the originating particles (so after meeting the horizontal vertex the outgoing particles have changed from the ingoing particles).

To determine whether the interaction (horizontal) is γ , W⁻ or W⁺ we must consult the laws of conservation of charge, baryon number and lepton number. The arriving particles are drawn from the bottom (before), the exiting particles to the top (after).





		Left	Right	Change	Left	Right	Change
Q	before	-1	-1	_	0	0	
	after	— 1	-1	-	+1	—1	+1-1=0
В	before	0	0	_	1	0	
	after	0	0	-	1	0	0
L_e	before	+1	+1	_	0	+1	
-	after	+1	+1	-	0	-1	+1-1=0
Exchange particle γ (no change		change)		W- (to balanc	e charge)	

The change in ${\rm L}_{\mu}$ and ${\rm L}_{\tau}$, which are not shown here, should also be 0 (= conservation)

7.6.6 Higgs particle

The theory of quarks, leptons and exchange particles defines the so-called Standard Model of particles and interactions. The centerpiece of this model is the Higgs particle, which is responsible through its interactions for the mass of the particles of the standard model.





ENERGY PRODUCTION



8.1. Energy sources	84
- Fossil fuels - Nuclear power - Solar power - Hydroelectric	
power - Wind power	
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8.2. Thermal energy transfer	09



8.1 Energy sources



Primary energy all types of unprocessed energy sources

Secondary energy processed or exploited to mechanical work or electrical form

ercize

- 1. Can you give two examples of each?
- 2. Estimate how much energy can we actually extract from primary energy sources?



Specific energy, E_s is the amount of energy that can be extracted from a unit mass of fuel

Energy density, E_D is the amount of energy that can be extracted from a unit *volume* of fuel

Table 8.1: Specific energy or energy density of fossil fuels

Fuel	Specific Energy $E_s/J \mathrm{kg}^{-1}$	Energy density $E_D/\mathrm{J}\mathrm{m}^{-3}$
uranium-235	7.0×10^{13}	1.3×10^{18}
hydrogen	1.4×10^{8}	1.0×10^{7}
natural gas	5.4×10^{7}	3.6×10^{7}
gasoline	4.6×10^{7}	3.4×10^{10}
kerosene	4.3×10^{7}	3.3×10^{10}
diesel	4.6×10^{7}	3.7×10^{10}
coal	3.2×10^{7}	7.2×10^{10}



Renerwable energy a fuel that is created faster or equally fast as it is consumed.

Non-renewable energy a fuel that is consumed faster than it is created.



8.1.1 Fossil fuels



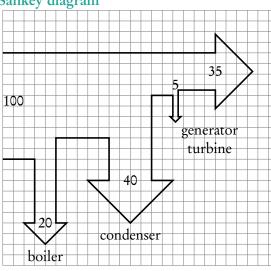
Fossil fuels are produced by the decomposition of buried animal and plant material due to pressure and bacteria

Table 8.2: Energy sources and the percentage of the total energy production for each. The third column gives the mass of carbon dioxide emitted per unit of energy produced from a particular fuel. Fossil fuels account for about 80% of the total energy production.

Fuel	Percentage of total energy production / %	Carbon dioxide emission / gMJ ⁻¹
oil	32	70
natural gas	21	50
coal	27	90
nuclear	6	_
hydroelectric	2	_
biofuels	10	_
oil	< 2	_

Given the environmental hazards of coal and oil, we will assume we can only use natural gas in the IB. To represent energy flows, we use a Sankey diagram





Given that:

$$efficiency = \frac{useful power}{input power}$$
$$power = \frac{energy}{time}$$

what is the efficiency of our power plant?

Advantages	Disdvantages
Cheap High power output	Fossils fuels will run out Environmental hazards
Ease of use	



8.1.2 Nuclear power

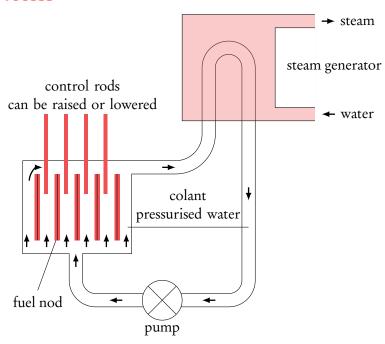


Nuclear power a nuclear reactor is a machine in which nuclear fission reactions take place producing energy.

The fuel used is uranium-235. Can you remember this reaction from the last topic?

$$^{1}_{0}n + ^{235}_{92}U \longrightarrow ^{141}_{56}Ba + ^{92}_{36}Kr + 3^{1}_{0}n$$

Reaction Process



This is a self sustained reaction, because it is a *chain reaction*. For the reaction to get going, we need to have minimum mass called the *critical mass* of uranium. To control the reaction, neutrons are slowed using a *moderator* which is usually a material surrounding the *fuel rods*. The moderator (usually graphite or water) will heat up and this heat may be extracted using a *heat exchanger*. finally, *control rods* may be introduced to absorb neutrons and thus decrease the rate of reaction.

Advantages	Disdvantages
High power output	Disposing of radioactive waste
Large reserves of nuclear fuels	Uranium mining
No greenhouse gases	Risk of nuclear explosion



8.1.3 Solar power



Solar power on a clear day earth receives $\sim 1000 \, \mathrm{W^2 \, m^{-1}}$ of energy from the sun. There are two methods for harnessing this energy.

Solar panels collect heat and water in pipes underneath is heated.

Photovoltaic cells convert light directly into electricity at an efficiency of $\sim 25\%$

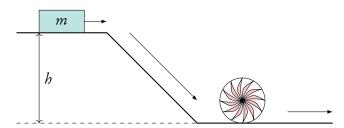
8.1.4 Hydroelectric power



Hydroelectric power Power derived from moving masses of water

Derivation

Water falls from a resevoir down to a power station. The water has a mass m and falls a height h.



- 1. The potential energy is mgh
- 2. $m = \rho \Delta V$, where $\rho =$ density, ΔV is volume.

3.
$$P = \frac{\Delta E}{\Delta t} = \frac{mgh}{\Delta t} = \frac{\rho \Delta Vgh}{\Delta t} = \rho gh \frac{\Delta V}{\Delta t}$$

- 4. $Q = \frac{\Delta V}{\Delta t}$ (volume flow rate)
- 5. $P = \rho Qgh$

What is the main problem with hydroelectric power?

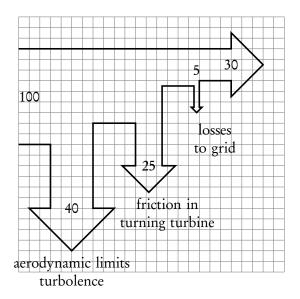


8.1.5 Wind power



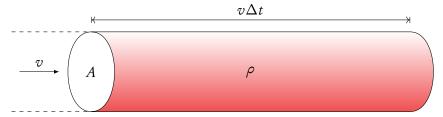
Wind power power derived from moving masses of air

Wind power speaks for itself. Given, we have all seen wind generators at some point. Typically about \sim 30% of the power carried in wind is converted to energy as shown by Sankey diagram below.



Derivation

Consider the mass of air that can pass through a tube of cross sectional area A with velocity v in time Δt . The air density is ρ



- 1. $m = \rho A v \Delta t$ (mass of air)
- 2. Kinetic energy of air is $E = \frac{1}{2}mv^2 = \frac{1}{2}\rho Av\Delta t v^2 = \frac{1}{2}\rho A\Delta t v^3$
- 3. Power = $\frac{E}{\Delta t} = \frac{1}{2} \rho A v^3$



Energy source	Advantages	Disdvantages
Solar	Cheap Renewable Clean	Low power output Inconsistent
Hydroelectric	Cheap Clean	Water storage Damage to local ecology
Wind	Clean Renewable	Large infrastructure Inconsistent

8.2 Thermal energy transfer

Heat can be transferred by three different methods.



Conduction is the transfer of energy due to high energy electrons colliding with neighbouring molecules.

Convection is is best explained by an example.

Air over a hot radiator in a room is heated, expands and rises, transferring warm air to the rest of the room. Cold air takes its place through convection currents and the process repeats.

Radiation is the transfer of energy through electromagnetic radiation.

Black-body radiation The power radiated by a body is governed by Stefan-Boltzman law

$$P = \text{power}$$

$$\varepsilon = \text{emissivity}$$

$$\sigma = \text{Stefan-Boltzmann constant}$$

$$A = \text{area}$$

$$T = \text{thermodynamic temperature [K]}$$

$$[J s^{-1}]$$

$$\sigma = Stefan - Boltzmann constant$$

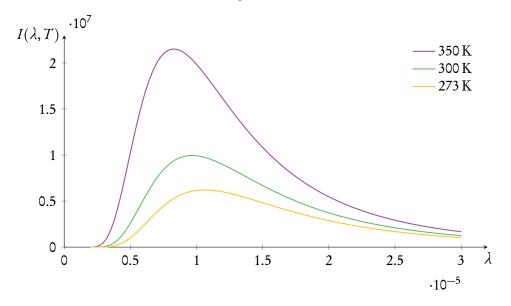
$$A = \text{fm}^{2}$$

$$T = \text{thermodynamic temperature [K]}$$

Emissivity ε measures how effectively a black-body radiates. $\varepsilon = 1 \Rightarrow$ black body.



Figure 8.1



Most energy is radiated at a specific wavelength λ_{max} determined by Wien's displacement law. For green box,

$$\lambda_{\rm max}T = 2.90 \times 10^{-3} \,\rm km$$

This is shown for various temperatures in the figure below.



Solar Constant Intensity is the power of radiation received per unit area.

$$I = \frac{P}{4\pi r^2 \sim 1400 \,\mathrm{W \, m^{-2}}}$$

This is the solar constant *S* and is the amount of solar radiation at the top of earth's atmosphere.

$$albedo = \frac{total\ scattered\ power}{total\ incident\ power}$$

Using the albedo we can find the average intensity incident on the earth.

$$I_{\text{avg}} = \frac{(1-\alpha)S}{4} = 245 \,\text{W m}^{-2}$$



Temperature at earth's surface

We are interested in average temperature at the Earth's surface. The earth radiates power from the entire surface area of its spherical shape, so the power radiated is

$$P_{\rm out} = \sigma A T^4$$

We are assuming earth to be black body so, $\varepsilon = 1$.

$$I_{\rm out} = \frac{P_{\rm out}}{A} = \sigma T^4$$

Equating the incident and outgoing intensities we get

$$\frac{(1-\alpha)S}{4} = \sigma T^4$$

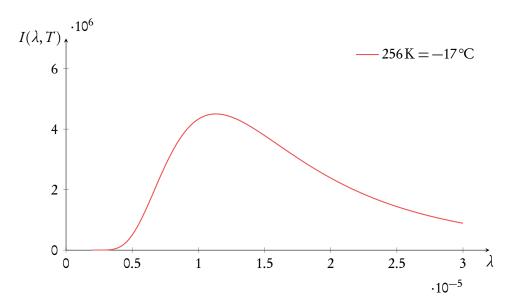
Solving the equation, we get

$$T = \sqrt[4]{\frac{(1-\alpha)S}{4\sigma}}$$

This evaluates to

$$T = \sqrt[4]{\frac{245}{5.67 \times 10^{-8}}} = 256 \,\mathrm{K}$$

This temperature is -17 °C.





Greenhouse effect Greenhouse gases strongly absorb infrared radiation from the atmosphere, when re-radiated in all directions, these gases account for additional warming. These gases include Water vapour, Carbon dioxide, Methane and Nitrous oxide.

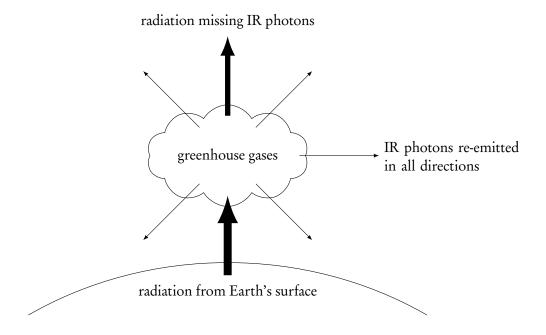


Table 8.3: Sources of greenhouse gases

Greenhouse gas	Natural Sources	Anthropogenic sources
H ₂ O	evaporation of water from oceans, rivers and lakes	irrigation
CO ₂	forest fires, volcanic eruptions, evaporation of water from oceans	burning fossil fuels in power plants and cars, burning forests
CH ₄	wetlands, oceans, lakes and rivers, termites	flooded rice fields, farm animals, procession of coal, natural gas and oil, burning biomass
N ₂ O	forests, oceans, soil and grasslands	burning fossil fuels, manufacture of cement, fertilizers, deforestation (reduction of nitrogen fixation in plants)

